# Nonadiabatic Molecular Dynamics Modeling of the Intrachain Charge Transport in Conjugated Diketopyrrolo-pyrrole Polymers

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**Supporting Information** 

**ABSTRACT:** Understanding the carrier transport processes and predicting the carrier mobility from first principle in organic electronic materials has been a longstanding challenge. We have applied the nonadiabatic Ehrenfest dynamics coupled with density functional tight binding (DFTB) to investigate the carrier motion in the donor– acceptor type polymer for photovoltaics. The equations of motion for the electrons are evolved under the fixed subspace spanned by the active molecular orbitals during each nuclear time step, and the feedback from charge to the nuclei motions, namely, the polaronic effect, is considered. We then use this methodology to investigate the charge transport dynamics for the ladder-type poly(*p*-phenylenes) (LPPP) and poly-(diketopyrrolo-pyrrole (DPP)) series with ~2 × 10<sup>3</sup> atoms. The carrier mobilities are evaluated via the diffusion process. It was found that the diffusion abilities are determined by the magnitude of transfer integrals



and localization length for frontier orbital, which is caused by the self-trapping effects (polaron) arising from the double bond stretching and twisting motions. This method can be useful in exploring the underlying charge transport behavior and improving the structure design of materials in organic electronics.

# 1. INTRODUCTION

Mobility is an important parameter to the performance of organic field effect transistors (OFETs), organic photovoltaics (OPVs)m and organic light emitting diodes (OLEDs).1-4 Recently, the DPP-based donor-acceptor conjugated copolymers have demonstrated mobility up to  $10 \text{ cm}^2/(\text{V s})$  for hole and 1 cm<sup>2</sup>/(V s) for electron in the OFETs.<sup>5–8</sup> Siebbeles et al. have combined the microwave experiment with one-dimensional diffusion model calculation and shown the mobility in LPPP is estimated to be  $\sim 600 \text{ cm}^2/(\text{V s})$ .<sup>9,10</sup> The most recent structure probe experiments indicate that the transport behavior in high mobility polymers presents quasi onedimensional; that is, carrier conduction is mostly along the backbone direction with very few intermolecular hopping through short  $\pi$ -orbital overlap.<sup>11-14</sup> Understanding the intrachain charge transport is the first step to improving the performance or design new material systems in the devices. Therefore, it is of great importance to develop ab initio dynamic methods to simulate the underlying charge transport process and to calculate the charge mobility.

Theoretically, on the basis of model Hamiltonian for organic crystals and conjugated polymers, the mixed quantum/classical (MQC) dynamics<sup>15</sup> have been used to investigate carrier transport mechanism and to evaluate the carrier mobility considering the intramolecular<sup>16</sup> and intermolecular<sup>17</sup> elec-

tron-phonon coupling effects. Most recently, Wang and Beljonne have developed the MQC flexible surface hopping dynamics to treat the crossover behavior from hopping to bandlike transport regimes in a unified way.<sup>18-20</sup> These methods have all treated the nuclear motions classically. However, the nuclear quantum tunneling effects have been found to be important for charge transport in organic semiconductors and conjugated polymers.<sup>21-23</sup> Nonperturbative hierarchically coupled equations of motion or non-Markovian stochastic Schrödinger equation, which can consider the nuclear quantum effect, have been successfully applied to carrier dynamics in molecular aggregates.<sup>24,25</sup> However, this is either computationally expensive or requires spectral density before the electron dynamics simulation, and also there is no explicit feedback effect from electron to the nuclear. From an ab initio point of view, the multiscale methods combined with static<sup>26</sup> and dynamic disorders<sup>27–29</sup> have been developed to study macroscopic transport behavior in poly(3-hexylthiophene) (P3HT). The intrinsic mobility in a 4802-atom system has been obtained directly by using an integrated tool consisting of large-scale electronic structure calculation, electron dynamics, and classical

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nuclear dynamics.<sup>30</sup> However, the feedback from electrons to the nuclei, that is, the polaronic effect, has been neglected. The recent advances in DFTB approach have been demonstrated as an effective method for treating electronic structure in complex systems.<sup>31–38</sup> Also, it has been successfully combined with MQC nonadiabatic molecular dynamics methods and found multiple applications for charge transfer in DNA,<sup>39–42</sup> non-radiative decay in water molecules,<sup>43</sup> biological basis,<sup>44–46</sup> and as organic molecule with counterintuitive aggregation-induced emission phenomena.<sup>47</sup>

In this work, we focus on the charge transport process in the intrachain conjugated polymer systems, which contain about  $10^3$  to 2  $\times$  10<sup>3</sup> atoms. The MQC Ehrenfest dynamics that can take into account the feedback from electrons to the nuclei have been implemented to investigate the detailed charge transport dynamics based on the DFTB electronic structure calculation. From the ensembles of trajectories in the nonadiabatic and Born-Oppenheimer dynamics, the results, such as carrier diffusion behavior, the evolutions of delocalization length for the frontier orbital and internal coordinates, density of states, and the energy autocorrelation functions (ACFs), can be analyzed. The mobilities for the polymers are evaluated directly from the diffusion processes. It is found that the double bond stretching and twisting motions related to the dithienyl-DPP unit mainly caused the orbital localization, modulated the transfer integrals, and affected the mobility in the conjugated polymer.

# 2. THEORETICAL METHODOLOGY

**2.1. Electronic Structure Calculation.** The dftb+ code,<sup>48</sup> which was integrated by the Ehrenfest nonadiabatic molecular dynamics, is used to calculate the electronic structure for the polymers on-the-fly. The *i*th molecular orbital  $|\varphi_i\rangle$  can be obtained from the Kohn–Sham (KS) equation  $\hat{H}|\varphi_i\rangle = \varepsilon_i|\varphi_i\rangle$ , where  $\varepsilon_i$  is the orbital energy for  $|\varphi_i\rangle$ . When expressed on atomic basis, the matrices equation HC = SCE is obtained, where *H* and *S* represent the Hamiltonian and overlap matrices, respectively. *C* and *E* denote wave function and molecular orbital energies. Both *H* and *S* are parametrized as a function of adjacent atomic distance for each atomic type. So it is highly efficient for the electronic structure calculation when running the dynamics on-the-fly. On the basis of the KS orbitals from DFTB, the evolution state  $|\varphi(t)\rangle$  can be constructed as:

$$|\psi(t)\rangle = \sum_{m=1}^{N} a_m(t) |\varphi_m(t)\rangle$$
(1)

 $a_m(t)$  is the evolution coefficient for the *m*th state at time *t*, and *N* is the total number of KS orbitals.

**2.2. Nonadiabatic Dynamics.** The evolution state  $|\psi(t)\rangle$  follows the time-dependent Kohn–Sham (TDKS) equation:

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H}(t) |\psi(t)\rangle$$
 (2)

From eqs 1 and 2, we obtain the TDKS equation:

$$i\hbar\frac{\partial}{\partial t}a_n = a_n\varepsilon_n - i\hbar\sum_m a_m\langle\varphi_n(t)|\frac{\partial}{\partial t}|\varphi_m(t)\rangle$$
(3)

Generally, the nonadiabatic coupling term  $\langle \varphi_n(t)|\partial/(\partial t)|\varphi_m(t)\rangle$ needs to be linearly interpolated between two adjacent time steps ([ $t_1$ ,  $t_2$ ]) for the nuclear. However, during these time steps, there are many energy level degenerations or crossings within KS orbitals for molecular systems in charge transport, so it is not appropriate to use eq 3 directly. We make the following expansion:

$$|\psi(t)\rangle = \sum_{m=1}^{N} a'_{m}(t)|\varphi_{m}(t_{1})\rangle$$
(4)

where *t* belongs to  $[t_1, t_2]$ , and the equation of motion can be written as:

$$i\hbar \frac{\partial}{\partial t} a'_{n}(t) = \sum_{m} a'_{m}(t) \langle \varphi_{n}(t_{1}) | \hat{H}(t) | \varphi_{m}(t_{1}) \rangle$$
$$\equiv \sum_{m} a'_{m}(t) H_{nm}(t)$$
(5)

In the following nonadiabatic molecular dynamics, eq 4 is used as the equation of motion for the electron. In this case, the space spanned by the basis  $\{|\varphi_1(t_1)\rangle, \dots |\varphi_m(t_1)\rangle, \dots, |\varphi_N(t_1)\rangle\}$  is fixed between  $[t_1, t_2]$ , so the numerical problem caused by energy level degeneration or crossing can be avoided. According to the linear-time-dependence approximation for H(t):<sup>30</sup>

$$H(t) = H(t_1) + \frac{t - t_1}{t_2 - t_1} [H(t_2) - H(t_1)]$$
(6)

where the matrix elements in Hamiltonian  $H(t_1)$  and  $H(t_2)$  can be written as:

$$H_{nm}(t_1) = \langle \varphi_n(t_1) | \hat{H}(t_1) | \varphi_m(t_1) \rangle = \delta_{nm}$$
<sup>(7)</sup>

and

$$H_{nm}(t_2) = \langle \varphi_n(t_1) | \hat{H}(t_2) | \varphi_m(t_1) \rangle \tag{8}$$

After the expansion:

$$|\varphi_k(t_2)\rangle = \sum_m b_{mk} |\varphi_m(t_1)\rangle \tag{9}$$

where  $b_{mk} = \langle \varphi_m(t_1) | \varphi_k(t_2) \rangle$ , the Gram–Schmidt orthogonalization is applied to  $b_{mk}$  as the restriction of orthonormal condition  $\langle \varphi_k(t_2) | \varphi_l(t_2) \rangle = \delta_{kl}$ . Next,  $H_{nm}(t_2)$  can be derived as

$$H_{nm}(t_{2}) = \sum_{kl} \langle \varphi_{n}(t_{1}) | \varphi_{k}(t_{2}) \rangle \langle \varphi_{k}(t_{2}) | \hat{H}(t_{2}) | \varphi_{l}(t_{2}) \rangle$$
$$\langle \varphi_{l}(t_{2}) | \varphi_{m}(t_{1}) \rangle$$
$$= \sum_{k} \varepsilon_{k}(t_{2}) b_{nk} b_{km}^{\dagger}$$
(10)

Substituting eq 6 with eqs 7 and 10, H(t) can be calculated through linear interpolation between  $H(t_1)$  and  $H(t_2)$ . From eqs 1, 4, and 9,  $|\psi(t_2)\rangle = \sum_m a'_m |\varphi_m(t_1)\rangle = \sum_i a_i |\varphi_i(t_2)\rangle = \sum_i a_i \sum_m b_{mi} |\varphi_m(t_1)\rangle$ , we can find the relationship between  $a'_m$ and  $a_i$ :

$$a'_m = \sum_i b_{mi} a_i \tag{11}$$

To study the charge transport, one electron or hole is added into the system, while the other electrons can be frozen at ground state approximately. In the framework of DFTB, under single electron approximation, the average electronic state energy including dynamic part and ground state part<sup>48</sup> plus nuclear repulsion energy  $E_{\rm rep}$  read as



Figure 1. The chemical structures for (a) LPPV, n = 60, (b) DPP\_DPP, n = 50, (c) DPP\_cTT, (d) DPP\_cDT, (e) DPP\_f3T, (f) DPP\_BDT, (g) DPP\_NPT, and (h) DPP\_CBZ; for (c)-(g), n = 32.

$$E^{\text{average}}(t) = E^{\text{dynamic}} + E^{\text{ground}}$$
  
=  $\langle \psi(t) | \hat{H} | \psi(t) \rangle$   
+  $\sum_{i} f_{i} \langle \varphi_{i}(t) | \hat{H}_{0} | \varphi_{i}(t) \rangle + \frac{1}{2} \sum_{\alpha, \beta} \gamma_{\alpha\beta} \Delta q_{\alpha} \Delta q_{\beta}$   
+  $E_{\text{rep}}$  (12)

where  $f_i$  is the occupation number for the *i*th orbital frozen at ground state, and  $\gamma_{\alpha\beta}$  is a parameter depending on the Hubbard parameters of atoms  $\alpha$  and  $\beta$  and the distance between the two atoms.  $\Delta q_{\alpha}$ ,  $\Delta q_{\beta}$  represent Mulliken charge fluctuations on isolated atoms  $\alpha$ ,  $\beta$ , respectively, and can be evaluated selfconsistently. Nuclei are treated classically and can be derived according to Newton equation of motion. The force  $\mathbf{F}_{\alpha}$  as the derivative of  $E^{\text{average}}$  in the Ehrenfest dynamics applied to the nuclear  $\alpha$  can be written as

$$\begin{aligned} \mathbf{F}_{\alpha} &= -\nabla_{\mathbf{R}_{\alpha}} E^{\text{average}}(t) = \mathbf{F}_{\alpha}^{\text{dynamic}} + \mathbf{F}_{\alpha}^{\text{ground}} \\ &= -\sum_{\mu\nu} \rho_{\nu\mu}'(t) \nabla_{\mathbf{R}_{\alpha}} H_{\mu\nu}^{0} - \left( \rho_{\nu\mu}'^{e}(t) - \frac{H_{\mu\nu}^{1}}{S_{\mu\nu}} \right) \nabla_{\mathbf{R}_{\alpha}} S_{\mu\nu} \\ &- \sum_{\mu\nu} \rho_{\nu\mu}'(t) \frac{1}{2} S_{\mu\nu} \nabla_{\mathbf{R}_{\alpha}} (\gamma_{\delta\alpha} + \gamma_{\beta\alpha}) \Delta q_{\alpha} \\ &- \sum_{\mu\nu} \rho_{\nu\mu}(t) \nabla_{\mathbf{R}_{\alpha}} H_{\mu\nu}^{0} - \left[ \rho_{\nu\mu}^{e}(t) - \frac{H_{\mu\nu}^{1}}{S_{\mu\nu}} \rho_{\nu\mu}(t) \right] \nabla_{\mathbf{R}_{\alpha}} S_{\mu\nu} \\ &- \Delta q_{\alpha}(t) \sum_{\zeta}^{N} \nabla_{\mathbf{R}_{\alpha}} \gamma_{\alpha\zeta} \Delta q_{\zeta}(t) - \nabla_{\mathbf{R}_{\alpha}} E_{\text{rep}} \end{aligned}$$
(13)

which is similar to the ground-state force calculation,<sup>48</sup> and the dynamic part  $\mathbf{F}_{\alpha}^{\text{dynamic}}$  from  $\langle \psi(t)|\hat{H}|\psi(t)\rangle$  can be derived and shown in the Supporting Information, where  $\rho_{\nu\mu'} \equiv \sum_{m} c_{\nu m} a_{m}^{\dagger}(t) a_{m}(t) c_{m\mu}^{\dagger}$ ,  $\rho_{\nu\mu}(t) \equiv \sum_{m} f_{m} c_{\nu m} c_{m\mu}^{\dagger}$  and  $\rho_{\nu\mu}^{\prime c} = \sum_{m} c_{\nu m} a_{m}^{\dagger}(t) e_{m} c_{m\mu}^{\dagger}$ ,  $\rho_{\nu\mu}^{\prime}(t) \equiv \sum_{m} f_{m} e_{m} c_{m\mu}^{\dagger}$  correspond to the density matrix and energy weighted density matrix, respectively.  $a_{m}(t)$  can be determined according to the electron equation of motion eqs 5 and 11.  $H_{\mu\nu}^{0} \equiv \langle \phi_{\mu} | \hat{H}_{0} | \phi_{\nu} \rangle$  and  $H_{\mu\nu}^{1} \equiv 1/2S_{\mu\nu} \sum_{\zeta}^{N} (\gamma_{\alpha\zeta} + \gamma_{\beta\zeta}) \Delta q_{\zeta}$  denote zero-order Hamiltonian and self-

consistent charge terms, respectively.<sup>48</sup> The density matrices are updated at each nuclear time step, and the derivatives of  $H^0_{\mu\nu}$ ,  $S_{\mu\nu}$ ,  $E_{\rm rep}$ , and  $\gamma_{\alpha\zeta}$  are evaluated numerically in the original dftb+ code; the parameter set mio-1-1 is used in this work.

#### 3. RESULTS AND DISCUSSION

3.1. Initial State for Electron Dynamics. To elucidate the structure-property relationship, we investigate eight kinds of single chain polymers with chemical structures shown in Figure 1. There are two kinds of homopolymers, LPPP and poly dithienyl-DPP (DPP\_DPP), consisting of 60 and 50 monomers, respectively. The rest are copolymers each with 32 monomers, which consist of the same acceptor dithienyl-DPP unit and different kinds of donor units as thienothiophene (DPP cTT), cyclopentadithiophene (DPP cDT), dithienothiophene (DPP\_f3T), benzodithiophene (DPP\_BDT), naphthalene (DPP\_NPT), and carbazole (DPP\_CBZ). The oligomer length is chosen according to the fact that the charged carrier is expected not to reach the boundary within the simulation time. There are about  $10^3$  to  $2 \times 10^3$  atoms in total for each polymer chain. We optimize the dimer structure using the Gaussian 09 package<sup>49</sup> with B3LYP functional and 6-31G(d, p) basis sets and extend to one-dimensional chain with the desired number of units. It should be noted that the side chain is neglected because we did not consider the intermolecular packings.  $^{7,50-54}_{\phantom{10}}$ 

We expand the hole wavepacket in the subspace of occupied orbitals. We choose 120 and 50 eigenstates for LPPP and DPP\_DPP, respectively, and 32 eigenstates for other copolymers. The charge conservation is carefully checked to ensure this subspace spanned by the eigenstates is complete for the expansion. The initial hole state is prepared with location at the central unit of the polymer through projecting the HOMO orbital in the monomer into the subspace. The charge mainly centers on the dithienyl-DPP unit, while it uniformly distributes along the central unit of the backbone for LPPP. The detailed charge distribution for the initial hole state of each polymer is shown in Figure S1 in the Supporting Information.

**3.2.** Nonadiabatic Dynamics for the Electrons and Nuclei. Considering the nonadiabatic dynamics, the initial velocities for the nuclei are randomly sampled according to Boltzmann distribution with temperature at 500 K. Because of the structure relaxation, the temperature will decrease to

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around 300 K at the diffusion region for the charge transport. After the initial conditions are assigned, the electron equations of motion are solved by the eighth order Runge-Kutta method with adjustable time step by using the rksuite 90 package,<sup>55</sup> while simultaneously the equations of motion for the nuclei are solved using the velocity Verlet algorithm with a time step of 0.5 fs. In this case, the polaron effect is naturally considered during the nonadiabatic dynamics. It is interesting to compare our result with that from literature, which has shown a negligible polaron effect on the charge transport in high mobility molecular systems based on the simulation with the Su-Schrieffer-Heeger (SSH) model.<sup>56</sup> Because of the differences in diffusion velocities for the polymers, the total time scale for each polymer is tested. Also, the time scales for LPPP, DPP DPP, and DPP cTT are 40, 50, and 60 fs, respectively, while for the other polymers it is 75 fs. The nonadiabatic molecular dynamics then are started from the initial conditions prepared above with 100 trajectories for each polymer. The number for the trajectory has been tested to ensure the convergence. The diffusion distance test for DPP CBZ copolymer with 50, 100, and 200 trajectories can be referred to as Figure 2S in the Supporting Information. In the following section, besides the ensemble averaging over 100 trajectories, we have also sampled enough number of points along each trajectory to the average.

The charge mobility can be evaluated from the nonadiabatic dynamics directly. First, the hole displacement  $\mathbf{r}(t)$  and square of the displacement  $\mathbf{r}^2(t)$  are approximately calculated by  $\mathbf{r}(t) = \langle \psi(t) | \mathbf{r} | \psi(t) \rangle \approx \sum_{\mu} |a_{\mu}(t)|^2 \mathbf{R}_{\alpha}$  and  $\mathbf{r}^2(t) = \langle \psi(t) | \mathbf{r} | \psi(t) \rangle \approx \sum_{\mu} |a_{\mu}(t)|^2 \mathbf{R}_{\alpha}^2$ , respectively. Second, the mean displacement (MD) and square of the displacement (MSD) are obtained through ensemble average over 100 trajectories. The variance of the displacement for the hole in each polymer is shown in Figure 2.



**Figure 2.** Variance of diffusion distance averaged from ensembles of 100 trajectories of the nonadiabatic dynamics for the LPPP, homo-DPP polymer (DPP DPP), and DPP copolymers, respectively.

There are three stages that can be found in the diffusion curve. It takes about 15 fs to experience the initial transition stage for each polymer. The curves in this stage are parabolic-like and similar to the inertial regimes for classical particles.<sup>57</sup> After that, the curves are linear versus time, suggesting that the diffusion regime takes over this stage. In about 5 fs, the hole will reach the chain end and go into the plateau regime. When the system evolves into the diffusion regime, the diffusion constant D = 1/ $2nt(\langle \mathbf{r}^2(t) \rangle - \langle \mathbf{r}(t) \rangle^2)$  (*n* is the dimension for the space) is evaluated by substituting the equation with MD and MSD for each polymer. Finally, according to the Einstein diffusion equation, the carrier mobility  $\mu = eD/k_{\rm B}T$ , where *e* is the charge for the carrier,  $k_{\rm B}$  is Boltzmann constant, and T is temperature. The intrachain hole mobilities obtained for each polymer are listed in Table 1. The mobility for LPPP is 50  $\text{cm}^2/(\text{V} \text{ s})$ , which is about 1 order of magnitude smaller than that by Siebbeles et al.9 In the latter work, first, the time-resolved microwave conductivity experiment was applied to measure the AC mobility for finite polymer chains. They observed chain length dependence for the high-frequency mobility. To consider the chain ends effect, the polymer chain then was modeled by a flat energy surface between infinitely high reflecting barriers, and the one-dimensional diffusion equation was used to obtain the charge carrier diffusion distance. In the end, the intrachain mobility for infinite chain length was extrapolated to be 600  $cm^2/(V s)$  based on the experimental results. However, in practical experiment, there is always a conjugation break existing in the polymer chains as shown by Scholes et al.<sup>58</sup> Besides, during the diffusion process, the energy surface for the charge carrier in the conjugated polymer is usually curved, not flat. For the DPP-based homopolymer, DPP DPP, the hole mobility is calculated to be 27  $\text{cm}^2/(\text{V s})$ . In the case of donoracceptor copolymer, the mobility depends on the kind of donor unit in the polymer chain. The highest and the lowest mobilities are 34 (DPP cTT) and 5 (DPP CBZ)  $cm^2/(V s)$ , respectively. It is found that hole mobility for donor-acceptor copolymers (except for DPP cTT) is usually less than homopolymer. This is in agreement with the microwave conductivity experiment for polydiacetylene-based copolymers.<sup>59</sup>

The delocalization length at the mobility edge is important to charge transport. The evolution of the highest occupied molecular orbital (HOMO) delocalization length (L) is shown in Figure 3a. The L is averaged from an ensemble of 100 trajectories for each polymer and calculated as  $L = 1/\sum_{\alpha=1}^{\infty} |$  $c_{\alpha}|^4$ , where  $c_{\alpha}$  is the wave function based on the  $\alpha$ th orthonormal atomic basis set. For all of the polymers considered here, the wave functions first localize in the initial  $\sim$ 5 fs, and then oscillate with decreased amplitude in the following evolution. The period for the oscillation is estimated to be 21 fs (~1587 cm<sup>-1</sup>) as indicated in the figure. This value suggests the importance of double bond stretching motion in coupling to the charge motion and causing the localization. The curves in the figure located from top to down correspond to the increasing wave function localization. Generally, this order is consistent with that for the magnitude of hole mobilities listed in Table 1; that is, the more delocalized is the orbital, the larger is the mobility for the polymer. To further illustrate the HOMO delocalization, the charge distributions along the

Table 1. Absolute Mobility for the Polymers Calculated from the Linear Region in Figure 2

	molecule									
	LPPP	DPP_DPP	DPP_cTT	DPP_cDT	DPP_f3T	DPP_BDT	DPP_NPT	DPP_CBZ		
mobility $(cm^2/(V s))$	50	27	34	25	20	14	11	5		



Figure 3. (a) HOMO delocalization (L) averaged over ensembles of 100 trajectories for the conjugated polymers, the oscillation period (~21 fs) corresponds to the stretching motion; and (b) charge distribution along the polymer chains with relevant L and estimated number of monomers. The values in the parentheses for L with I and II for each polymer are sampled at 10 and 25 fs in (a) corresponding to the most delocalized and localized band edge state.

polymer chains are plotted in Figure 3b. The numbers of monomers occupied by the orbitals are estimated and with their corresponding value of L are also shown in the parentheses for

each polymer in Figure 3b. The red color indicates the charge distribution. So it can be seen from Figure 3a and b that the effective conjugation lengths are within 15-9 monomers for

LPPP, 8-5 for DPP\_DPP, while in copolymers they are within 8-4 for DPP\_cTT, 5-3 for DPP\_NDT, 4-2 for DPP\_f3T, 4-2 for DPP\_BDT, 3-2 for DPP\_NPT, and 2-1 for DPP\_CBZ during the diffusion regime.

The densities of states (DOS) for the energies from the top 32 valence orbitals sampled from all of the trajectories are plotted in Figure 4a for LPPP and in Figure 4b for polymers



Figure 4. Densities of states from the top 32 valence orbital energies for different polymers.

with DPP unit. The energies are sampled from the diffusion regime during the nonadiabatic dynamics, and the DOS are obtained by directly counting the number of states falling between the given energy intervals. Two tails can be found at each side of the DOS profile for each polymer. These tail states can be attributed to fluctuations of orbital energies at the band edge. The higher mobility system favors a shallower band edge. Here, the contribution from the fluctuations of HOMO orbital energies to the total DOS is shown in Figure 3S in the Supporting Information. The DOS for HOMO follow Gaussian distribution. The full width at half-maximum (fwhm) estimated for HOMO is about 60–100 meV for each polymer. The fwhms for the total orbitals considered are listed in Table 2. There are two factors contributing to the broadening of energy levels. One is the renormalization by the electron–phonon couplings; the other comes from the orbital interactions, transfer integral. To gauge the relative contributions, that the bandwidths evolve with time is plotted in Supporting Information Figure 4S. The bandwidths oscillate with a period of  $\sim 20$  fs, which is in agreement with the double bond stretching mode. The largest amplitude for the oscillation is estimated to be ~55 meV. So it means the magnitude from electron-phonon coupling in different polymers is comparable and estimated to be several dozens of millielectronvolt. So the bandwidths listed in Table 2 corresponding to the broadening of total energy levels largely governed the transfer integral between adjacent monomer in the polymer. The larger bandwidth presents larger transfer integral and then shows higher charge mobility in the polymer. The mobilities versus bandwidths are plotted in Supporting Information Figure 5S. The relationship appears to be roughly linear, which is consistent with the diffusion behavior for charge carrier in a strong electronic coupling regime.

Now we discuss the evolution of typical dihedral angles and bond lengths, which have been taken as an ensembles average from 100 trajectories. The positions for the typical internal coordinates are labeled with red in the chemical structures and are shown in the insets in Figure 5a-f. The standard deviation (SD) of dihedral angles  $\sigma_1$  and  $\sigma_2$  versus time is plotted in Figure 5a and b, respectively. The dihedral angle  $\sigma_1$  in LPPP denotes the twisting motion between two adjacent benzene rings. In the first 15 fs, the SD of  $\sigma_1$  in LPPP increases fast to  $6^{\circ}$ , and then it keeps at this degree with small oscillations. When considering P-DPPs, the SDs of  $\sigma_1$ , which denote the twisting motion of thiophene rings in the DPP unit, increase fast to  $\sim 8^{\circ}$  in less than 15 fs and then increase slowly with fluctuations between  $\sim 5^{\circ}$  and  $\sim 10^{\circ}$ . Similarly, in Figure 5b, there are also two stages that can be found for rotations of  $\sigma_2$ . In LPPP, the dihedral angles represent the out-of-plane torsion for benzene rings with amplitude from  $\sim -4^{\circ}$  to  $\sim 4^{\circ}$ . In P-DPPs, the dihedral angles represent the rotations between DPP units and donor units. In the first 15 fs, these angles rotate with fast increasing amplitudes up to  $6^\circ$ ; in the following periods, the amplitudes change slowly up to the range of  $\sim 10^{\circ}$  at the end of the simulation time. Although the fluctuation amplitudes of  $\sigma_1$ and  $\sigma_2$  are within ~10°, the transfer integrals could take significant decrement because of the randomness for the distribution of the angles.<sup>60,61</sup> Also, it is anticipated that these torsions can further take an important part in localizing the charge distribution and coupling to the carrier motion corresponding to the diffusion regime as shown in Figures 2 and 3.

The stretching motions for different bonds are appended in Figure 5c–e. For LPPP, as shown in Figure 5c and d, the bond lengths are ~1.47 and ~1.40 Å with oscillation frequencies of ~24 fs (1388 cm<sup>-1</sup>) and ~19 fs (1754 cm<sup>-1</sup>), respectively. The oscillation amplitudes change ~0.01 Å during the diffusion regime. For the P-DPPs, the C=C stretching motions in Figure 5c and d show obvious increments in oscillation amplitudes with frequencies of ~23 fs (1449 cm<sup>-1</sup>). Similar behavior could also be found for C–N stretching motion with

Table 2. Bandwidth for the Polymers Estimated from the Full-Width at Half-Maximum (fwhm) in Figure 4

		molecule									
	LPPP	DPP_DPP	DPP_cTT	DPP_cDT	DPP_f3T	DPP_BDT	DPP_NPT	DPP_CBZ			
fwhm (meV)	600	370	365	377	362	279	268	242			



**Figure 5.** Temporal evolution of standard deviation for the typical dihedral angles for (a)  $\sigma_1$ , (b)  $\sigma_2$ , and average bond lengths for (c) C=C, (d) C=C, (e) C=N, and (f) C=O indicated with red color in the chemical structures for different polymers in the insets.

frequency of ~32 fs (1042 cm<sup>-1</sup>) in Figure 5e. Interestingly, the inverse process with decreasing amplitude can be found for C=O stretching motion of ~20 fs (1666 cm<sup>-1</sup>). The increasing and decreasing amplitudes indicate the excitation and relaxation processes for the vibrational modes. Also, the locations for these bonds are in general consistent with the charge distributions as shown in Figure 3b and Supporting Information Figure 1S. Combing these two aspects, we can infer that the feedback from electrons to the phonons is important and the polaronic effect cannot be neglected during the carrier diffusion in the P-DPPs.

**3.3. Born–Oppenheimer Dynamics.** To identify the overall phonon modes contributing to the electron–phonon couplings, the ACFs for the HOMO energy levels and the correspond Fourier transformed (FT) results are reported in

Figure 6. The ACFs are obtained by starting the Born– Oppenheimer dynamics with a time scale of 400 fs and a step of 0.1 fs for the nuclear motion. The initial settings for the geometries, velocities, and temperature are the same as the nonadiabatic dynamics. The ACFs can be calculated as:

$$ACF = \frac{\langle C_{EE}(n\Delta t) \rangle}{\langle C_{EE}(0) \rangle}$$
(14)

where

$$C_{EE}(n\Delta t) = \frac{1}{M-n} \sum_{m=1}^{M-n} E(m\Delta t)E((m+n)\Delta t)$$
(15)

*E* is the HOMO energy, *M* is the number for the total sampling points along the trajectory, and  $\Delta t$  is the nuclear time step. The



**Figure 6.** The Fourier transforms (FT) of the energy autocorrelation functions (ACFs) from Born–Oppenheimer dynamics. The corresponding ACFs are shown in the insets.

ACFs show fast decay (<10 fs) and oscillations around zero value, which indicate the possible thermal fluctuations caused memory loss and the establishments of equilibrium states. For P-DPPs, the peaks ranging from  $\sim$ 1400 to  $\sim$ 1800 cm<sup>-1</sup> can be attributed to C=C and C=O stretching motions, while the modes from ~1100 to ~1300 cm<sup>-1</sup> probably come from the single bonds stretching motions like C-N, C-C. One example for the C-N stretching is shown in Figure 5e. The low frequencies with wavenumber less than 300 cm<sup>-1</sup> give longer than 100 fs rotation periods. The peaks located at this region show small values except for DPP CBZ. Similar results can be found in LPPP, which show much smaller low frequency contributions because of the locking by the single bonds for the torsions. From the frequency domain results, we can find that the stretching motions with high frequencies take a major part in electron-phonon coupling, while the torsions with low frequencies take a minor part except for DPP CBZ.

# 4. CONCLUSIONS

To summarize, we have carried out a nonadiabatic dynamics simulation considering polaronic effects for the hole transport in polymer chains of LPPP and P-DPPs with  $10^3$  to  $2 \times 10^3$  atoms. The charge mobilities are calculated according to the Einstein diffusion equation through fitting the linear region of

diffusion curves. We find that the intrachain mobility in LPPP is ~50 cm<sup>2</sup>/(V s), while in P-DPPs it ranges from ~30 to ~5  $cm^2/(V s)$  depending on the different donor units. There are two major effects that contribute to the differences in transport abilities. One is the strength of transfer integral between the adjacent monomers, which is modulated by the random fluctuations of typical dihedral angles. The other is the localization length for frontier orbital, which is determined by the strength of electron-phonon couplings induced by the stretching and twisting motions related to DPP units. Our work demonstrated that this methodology is useful in understanding the charge transport process and predicting the mobility from first principle. However, there are two points that should be noted when predicting the carrier mobility. One is our investigation here is confined to a single polymer chain. The interaction of the charge carriers with their polar dielectric environment is neglected now, which can be very important to charge transport as shown by experimental and other theoretical works, in which the interactions have been described in the form of Fröhlich polaron.<sup>62-65</sup> The other is that the simulation now is focusing on intrachain transport, "through bond" diffusion. The "through space" component arising from coupled polymer segments is often the velocity deterministic step during the charge transport, so it is also very important to the mobility prediction. The interchain charge transport in "kinked" chains is being actively pursued.

# ASSOCIATED CONTENT

#### **S** Supporting Information

Additional details about derivation of force calculation from dynamic part, the charge distribution of initial hole wavepacket, the convergence test for diffusion distance in DPP\_CBZ copolymer, the contribution of HOMO in the total orbital DOS distribution, time evolution for the bandwidth, and the relationship between charge mobility and bandwidth in different copolymers. This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes

The authors declare no competing financial interest.

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